

**Mark Scheme 4725
January 2006**

Mark Total

1.	(i) $\frac{2 + 16i - i - 8i^2}{10 + 15i}$ (ii) $\frac{1}{5}(10 + 15i)$ or $2 + 3i$	M1 A1 M1 A1 A1ft	2 3 5	Attempt to multiply correctly Obtain correct answer Multiply numerator & denominator by conjugate Obtain denominator 5 Their part (i) or $10 + 15i$ derived again / 5
2.	$1^2 = \frac{1}{6} \times 1 \times 2 \times 3$ $\frac{1}{6}n(n + 1)(2n + 1) + (n + 1)^2$ $\frac{1}{6}(n + 1)(n + 2)\{2(n + 1) + 1\}$	B1 M1 DM1 A1 A1	 5 5	Show result true for $n = 1$ or 2 Add next term to given sum formula, any letter OK Attempt to factorise or expand and simplify Correct expression obtained Specific statement of induction conclusion, with no errors seen
3.	(i) $2 \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix} - 1 \begin{bmatrix} 1 & 1 \\ 1 & 3 \end{bmatrix} + 3 \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix}$ $2 \times 5 - 1 \times 2 + 3 \times -1$ 5 (ii)	M1 A1 A1 B1ft	 3 1 4	Show correct expansion process, allow sign slips Obtain correct (unsimplified) expression Obtain correct answer State that M is non-singular as $\det \mathbf{M}$ non-zero, ft their determinant
4.	$u^2 + 4u + 4$ $u^3 + 6u^2 + 12u + 8$ $u = \sqrt[3]{5}$ $x = 2 + \sqrt[3]{5}$	B1 M1 A1 A1ft A1ft	 5 5	$u + 2$ squared and cubed correctly Substitute these and attempt to simplify Obtain $u^3 - 5 = 0$ or equivalent Correct solution to their equation Obtain 2 + their answer [Decimals score 0/2 of final A marks]

5.	$8\Sigma r^3 - 6\Sigma r^2 + 2\Sigma r$ $8\Sigma r^3 = 2n^2(n+1)^2$ $6\Sigma r^2 = n(n+1)(2n+1)$ $2\Sigma r = n(n+1)$ $2n^3(n+1)$	M1	6	Consider the sum of three separate terms
		A1		Correct formula stated or used a.e.f.
		A1		Correct formula stated or used a.e.f.
		A1		Correct term seen
		M1		Attempt to factorise or expand and simplify
		A1		Obtain given answer correctly
	AG		6	

6.	<p>(i) $\frac{1}{2} \begin{pmatrix} 8 & -2 \\ -3 & 1 \end{pmatrix}$</p> <p>(ii) Either</p> $\frac{1}{2} \begin{pmatrix} 14 & 2 \\ -5 & 0 \end{pmatrix}$ <p>Or</p> $\frac{1}{5} \begin{pmatrix} 3 & -1 \\ -1 & 2 \end{pmatrix}$ $\mathbf{B} = \mathbf{A}^{-1} \mathbf{C}$ $\mathbf{B} = \frac{1}{5} \begin{pmatrix} 0 & -2 \\ 5 & 14 \end{pmatrix}$ $\frac{1}{2} \begin{pmatrix} 14 & 2 \\ -5 & 0 \end{pmatrix}$ <p>Or</p> $\mathbf{AB} = \begin{pmatrix} 2a + c & 2b + d \\ a + 3c & b + 3d \end{pmatrix}$ $a = 0, c = 1, b = -0.4, d = 2.8$ $\frac{1}{2} \begin{pmatrix} 14 & 2 \\ -5 & 0 \end{pmatrix}$	B1	2	Transpose leading diagonal and negate other diagonal
		B1		Divide by determinant
		B1	5	State or imply $(\mathbf{AB})^{-1} = \mathbf{B}^{-1} \mathbf{A}^{-1}$
		M1A1		Use this result and obtain $\mathbf{B}^{-1} = \mathbf{C}^{-1} \mathbf{A}$, or equivalent matrix algebra
		M1	5	Matrix multn., two elements correct, for any pair
		A1ft		All elements correct ft their (i)
		B1		Find \mathbf{A}^{-1}
		M1		Premultiply by \mathbf{A}^{-1} stated or implied
		M1		Matrix multn. Two elements correct
		A1ft		All elements correct
		A1		Correct \mathbf{B}^{-1}
		B1		Find \mathbf{AB}
M1		Solve one pair of simultaneous equations		
A1A1		Each pair of answers		
A1		Correct \mathbf{B}^{-1}		
		7		

7.	<p>(a) (i) $\sqrt{13}$</p> <p>(ii)</p> <p>- 0.59</p> <p>(b)</p> <p>$1 - 2i$</p> <p>(c)</p>	<p>B1</p> <p>M1 A1 A1</p> <p>M1</p> <p>A1A1 A1</p> <p>B1 B1</p>	<p>1</p> <p>3</p> <p>4</p> <p>2</p> <p>10</p>	<p>Obtain correct answer, decimals OK</p> <p>Using $\tan^{-1}b/a$, or equivalent trig allow + or - Obtain 0.59</p> <p>Obtain correct answer</p> <p>Express LHS in Cartesian form & equate real and imaginary parts Obtain $x = 1$ and $y = -2$</p> <p>Correct answer written as a complex number</p> <p>Sketch of vertical straight line Through $(-0.5, 0)$</p>
8.	<p>(i)</p> <p>$\begin{pmatrix} 0 \\ 0 \end{pmatrix} \begin{pmatrix} 2 \\ 0 \end{pmatrix} \begin{pmatrix} 2 \\ -2 \end{pmatrix} \begin{pmatrix} 0 \\ -2 \end{pmatrix}$</p> <p>(ii) Either $\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$</p> <p>$\begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix}$</p> <p>Or $\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$</p> <p>$\begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix}$</p> <p>Or $\begin{pmatrix} 2 & 0 \\ 0 & 1 \end{pmatrix}$</p> <p>$\begin{pmatrix} 1 & 0 \\ 0 & -2 \end{pmatrix}$</p>	<p>B1</p> <p>B1 B1</p> <p>B1,B1 B1</p> <p>B1,B1 B1</p> <p>B1,B1 B1</p> <p>B1,B1 B1</p> <p>B1,B1 B1</p>	<p>3</p> <p>6</p> <p>6</p> <p>9</p>	<p>For correct vertex $(2, -2)$</p> <p>For all vertices correct For correct diagram</p> <p>Reflection, in x-axis Correct matrix</p> <p>Enlargement, centre O s.f. 2 Correct matrix</p> <p>Reflection, in the y-axis Correct matrix</p> <p>Enlargement, centre O s.f. -2 Correct matrix</p> <p>Stretch, in x-direction s.f. 2 Correct matrix</p> <p>Stretch, in y-direction s.f. -2 Correct matrix</p>

9.	<p>(i) $\frac{r+2-r}{r(r+2)}$ $\frac{2}{r(r+2)}$</p> <p style="text-align: center;">AG</p> <p>(ii)</p> $\frac{3}{2} - \frac{1}{n+1} - \frac{1}{n+2}$ <p>(iii) (a)</p> $\frac{3}{2}$ <p>(b)</p> $\frac{1}{n+1} + \frac{1}{n+2}$	<p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p> <p>B1ft</p> <p>M1</p> <p>A1 ft</p>	<p>2</p> <p>5</p> <p>1</p> <p>2</p> <p>10</p>	<p>Show correct process for subtracting fractions</p> <p>Obtain given answer correctly</p> <p>Express terms as differences using (i)</p> <p>Express 1st 3 (or last 3) terms so that cancelling occurs</p> <p>Obtain $1 + \frac{1}{2}$</p> <p>Obtain $-\frac{1}{n+2}, -\frac{1}{n+1}$</p> <p>Obtain correct answer in any form</p> <p>Obtain value from their sum to n terms</p> <p>Using (iii) (a) – (ii) or method of differences again [$n \rightarrow \infty$ is a method error]</p> <p>Obtain answer in any form</p>
10.	<p>(i) $\alpha + \beta + \gamma = 9$</p> <p>(ii)</p> $p = \frac{9 - \alpha}{2}$ <p>(iii) $\alpha\beta\gamma = 29$</p> <p>(iv)</p> $\alpha(p^2 + q^2) = 29$ $q = \sqrt{\frac{29}{\alpha} - \frac{(9 - \alpha)^2}{4}}$ <p>(iv) Alternative method</p> $2p\alpha + p^2 + q^2 = 27$ $q = \sqrt{27 - \frac{(9 - \alpha)^2}{4} - \alpha(9 - \alpha)}$	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1ft</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>1</p> <p>4</p> <p>1</p> <p>5</p> <p>11</p>	<p>State or use other root is $p - iq$</p> <p>Substitute into (i)</p> <p>Obtain $2p + \alpha = 9$</p> <p>Obtain correct answer a.e.f.</p> <p>Substitute into (iii)</p> <p>Obtain unsimplified expression with no i's</p> <p>Rearrange to obtain q or q^2</p> <p>Substitute their expression for p a.e.f.</p> <p>Obtain correct answer a.e.f.</p> <p>Substitute into $\alpha\beta + \beta\gamma + \gamma\alpha = 27$</p> <p>Obtain unsimplified expression with no i's</p> <p>Rearrange to obtain q or q^2</p> <p>Substitute their expression for p a.e.f.</p> <p>Obtain correct answer a.e.f.</p>